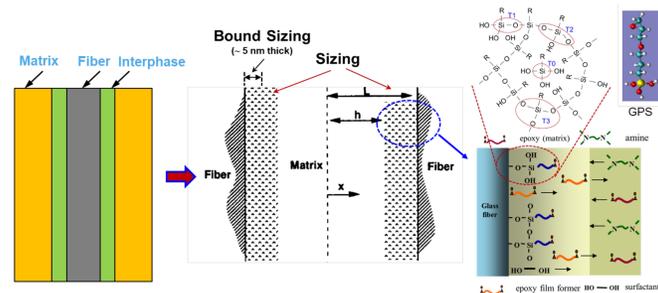


# Strain Rate Dependent Cohesive Traction Laws for Glass Fiber-Epoxy Interphase using Molecular Dynamics Simulations

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## Introduction

- In the glass fiber-epoxy composite, interphase is a distinct region between fiber and epoxy matrix that develops during processing through diffusion and reaction between the matrix and the fiber sizing
- Interphase could have different morphology depending on processing and thickness could vary from few nanometers to tens of nanometers
- Since load is transferred through interphase, it controls composites strength, toughness, and damage modes
- In high-velocity impact, interphase could be subjected up to  $1e12/s$  strain rate, and like many other materials interphase properties are also strain rate dependent
- Therefore, it is essential to understand the interphase properties tailoring mechanism at the atomistic scale as well as its strain rate-dependent responses



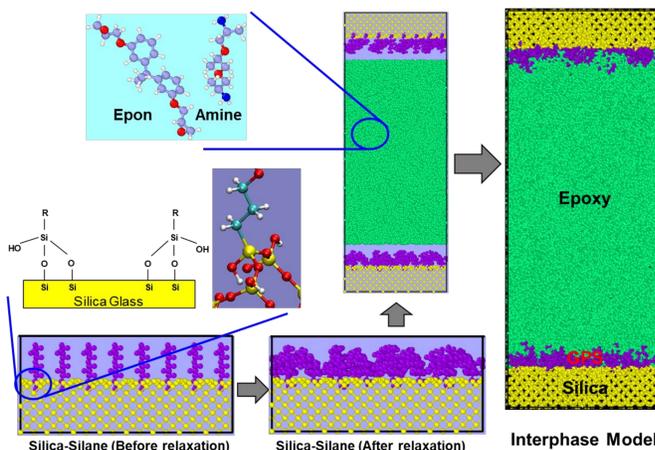
Fiber-Matrix Interphase System

## Objectives

- Establish a molecular dynamics (MD) based "Materials-by-Design" framework for composite interphase
- Develop strain-rate dependent traction law to bridge length scales in the finite element (FE) based continuum level micro-mechanics modeling of composites

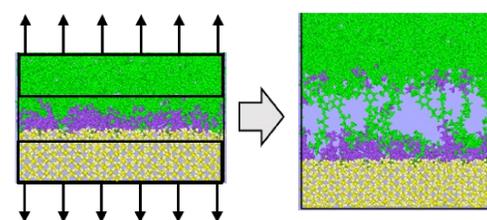
## Simulations Details

- We develop fiber-epoxy interphase with mono-layer 3-glycidoxypropyltrimethoxy silane (GPS)
- First, we deposit hydroxylated mono-layer silane on the silica surface at different number densities ( $0/nm^2$  to  $3.9/nm^2$ ) and react them with the silica surface through condensation reaction
- In the second step, a mixture of the Epon828-Jeffamine® D-230 is put on the silica slab, equilibrated, and cured
- Condensation and curing reaction are modeled with AMBER based cross-linking algorithm
- The model is then equilibrated with reactive force field ReaxFF before being subjected to mechanical loading



Interphase Model Development Procedure

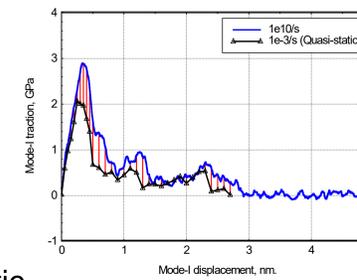
- Interphase thickness is determined from the Root Mean Squared Fluctuation method
- Interphase thickness is in the range of 1.3 to 1.7 nm for mono-layer silane



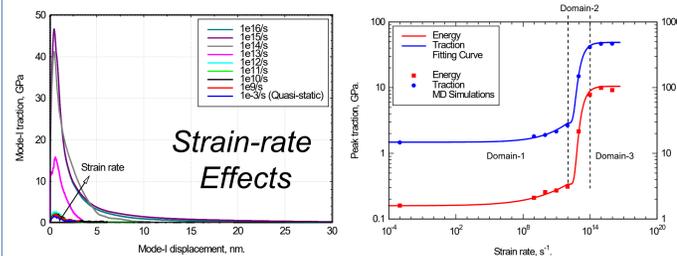
Mode-I Loading

## Results and Discussion

- Interphase is loaded in Mode-I at strain rates  $1e9/s$  to  $1e16/s$  including quasi-static loading
- Quasi-static response is determined from the tens of relaxation simulations at different deformation states
- Irrespective of interphase topology, peak traction and energy are highly strain-rate dependent and show characteristic S-shape response



Quasi-Static Response



Strain-rate Effects

- We successfully established the correlation between peak traction and energy as a function of silane number density and strain rate with the following equations.

Peak Traction: 
$$T = [T_{0,QS}(1 + a_T * D_{SN})][1 + b_T \epsilon^{c_T}], \text{ for } \epsilon \leq 1e12/s \quad (1a)$$

$$T = [T_{0,QS}(1 + a_T * D_{SN})][1 + b_T \epsilon^{c_T}] + [g_T + h_T * D_{SN}] \exp(-m_T - n_T * D_{SN}) \epsilon / \epsilon_{2,T}, \text{ for } \epsilon > 1e12/s \quad (1b)$$

Energy: 
$$G = [G_{0,QS}(a_{1,G} - (a_{1,G} - a_{2,G}) \exp(-D_{SN}/a_{3,G}))][1 + b_G \epsilon^{c_G}], \text{ for } \epsilon \leq 1e12/s \quad (2a)$$

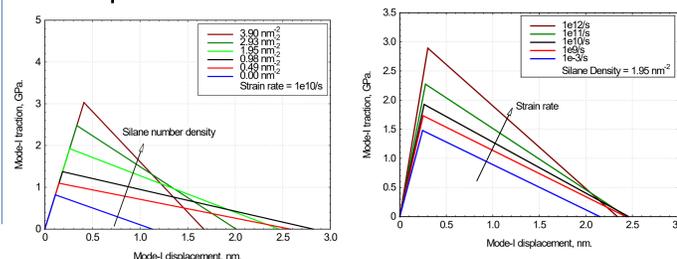
$$G = [G_{0,QS}(a_{1,G} - (a_{1,G} - a_{2,G}) \exp(-D_{SN}/a_{3,G}))][1 + b_G \epsilon^{c_G}] + [g_G + h_G * D_{SN}] \exp(-m_G - n_G * D_{SN}) \epsilon / \epsilon_{ref,G}, \text{ for } \epsilon > 1e12/s \quad (2b)$$

Stiffness: 
$$K = [K_{QS} + a_K \epsilon^{b_K}], \text{ for } \epsilon \leq 1e12/s \quad (3a)$$

$$K = [K_{QS} + a_K \epsilon^{b_K}] + c_K \exp(-\epsilon / \epsilon_{2,K}), \text{ for } \epsilon > 1e12/s \quad (3b)$$

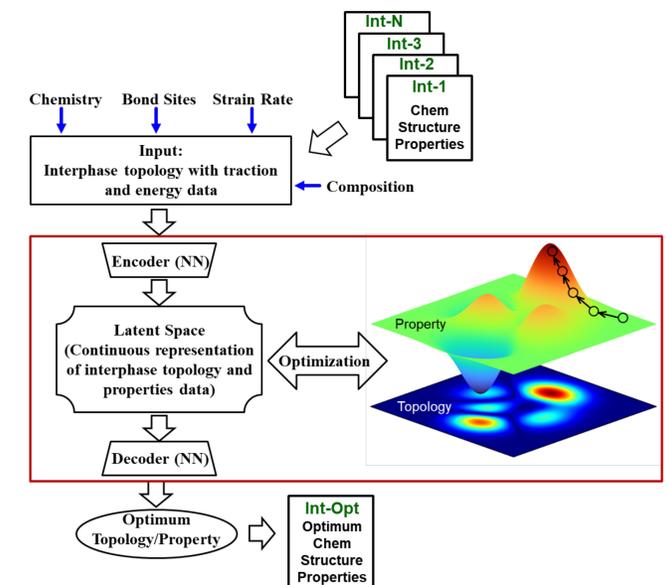
T is the traction, G is the energy,  $\epsilon$  is the strain rate,  $D_{SN}$  is the silane number density,  $T_{0,QS}$  and  $G_{0,QS}$  are the quasi-static traction and energy for the interphase without silane.

- The above correlations are used to predict simplistic bi-linear traction laws to use in FEA



## Path Forward

- We are in the process of developing strain-rate-dependent mixed-mode traction law
- Develop physics informed machine learning framework to design composite interphase for optimum strength and energy considering variability in interphase chemistry, topology, and strain rate



## References

- Chowdhury et al., Glass fiber-epoxy interactions in the presence of silane: A molecular dynamics study, Applied Surface Science 2021, 542:148738
- Chowdhury et al., Strain-Rate Dependent Mode I Cohesive Traction Laws for Glass Fiber-Epoxy Interphase using Molecular Dynamics Simulations. Composites Part B 2022, 237:109877

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