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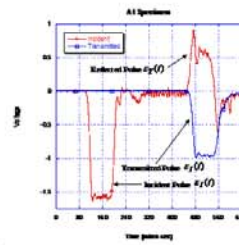
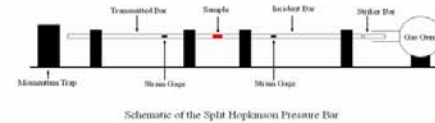
MOTIVATION

Motivation: Frequently high strain rate properties (i.e. modulus) obtained from Split Hopkinson Pressure Bar experiments do not match published values for materials

Objective: Accurately determine high strain rate dynamic compressive properties of a material using the Split Hopkinson Pressure Bar

- Minimizing errors inherent to the testing process
 - Wave dispersion
 - Variable strain-rate
 - Specimen surface finish
- Minimizing errors in the analysis
 - Time shift
 - Dispersion correction
 - Correct strain calculation

SPLIT HOPKINSON PRESSURE BAR CLASSIC METHODOLOGY



Classic 1-Wave Analysis

$$\epsilon_{s,cl}(t) = \frac{2c}{H} \int_0^t \epsilon_R(t) dt$$

$$\sigma_{s,cl}(t) = E_{Bar} \frac{A_{Bar}}{A_s} \epsilon_T(t)$$

Velocity of sound in the bar must be less than the velocity of sound in the specimen, $c_b < c_s$

SPLIT HOPKINSON PRESSURE BAR NEW METHODOLOGY

What if the velocity of sound in the bar is greater than the velocity of sound in the specimen? $c_b > c_s$

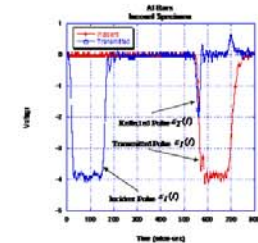
$$r = \frac{\rho_S c_S - \rho_B c_B}{\rho_S c_S + \rho_B c_B}$$

$$K_S = \frac{(1-r)^2}{4r}$$

$$K_S^{dyn} = \frac{(1+5r)(1-r)^3}{4r(1+r)^2}$$

$$\langle \epsilon_S(n\bar{T}) \rangle_{n=1}^N = K_S \cdot \langle \epsilon_S^{cl}(n\bar{T}) \rangle_{n=1}^N + K_S^{dyn} \cdot \frac{\rho_S}{\rho} \cdot \langle \epsilon_R(n\bar{T}, 0) \rangle_{n=1}^N$$

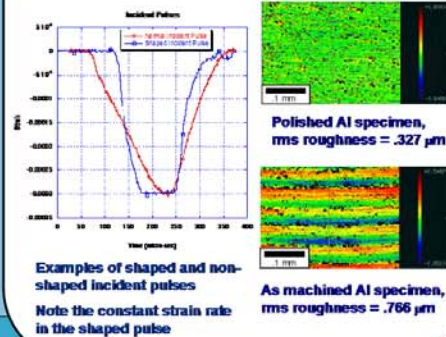
$$\langle \Sigma_S(n\bar{T}) \rangle_{n=1}^N = E \langle \epsilon_T(n\bar{T}, H) \rangle_{n=1}^N + E \frac{\rho_S}{2\rho} \cdot r \cdot \left\langle \frac{d}{d(n\bar{T})} \epsilon_T(n\bar{T}, H) \right\rangle_{n=1}^N$$



TESTING PARAMETERS

- Wave dispersion correction
 - All bars are dispersive in nature
 - Dispersion correction predicts the waves at the bar-specimen interfaces
- Pulse shaping
 - Creates a slowly rising incident pulse
 - Constant deformation over duration of pulse
 - Eliminates premature failure in brittle materials
 - Able to tailor stress level in specimen
 - Constant strain rate
 - Reduces high frequency oscillations, minimizing dispersion effects
- Time shift
 - Shifts all data to the same time domain
- Similar bar-specimen diameter ratio
- Specimen surface finish

TESTING PARAMETERS

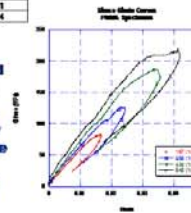


EXPERIMENTAL RESULTS

All Specimens, 1-68 GPa	
1-Wave Classic Analysis	
Specimen:Bar Diameter Ratio	Modulus (GPa)
0.5	58.9
0.7	61.2
0.8	65.5
0.9	65.9
1	68.7
100-1200 Analysis	
Specimen:Bar Diameter Ratio	Modulus (GPa)
0.5	58.4
0.7	59.2
0.8	64.0
0.9	63.1
1	66.4

Results show how specimen-bar diameter ratio affects modulus

PMMA specimens tested at different strain rates
 Future Work: Develop a technique for accurately determining the high rate properties of a visco-elastic material (PMMA)



CONCLUSIONS

Criteria for correct measurement of modulus

- The specimen-bar diameter ratio must be close to 1
- Specimens must be polished
- Pulse shaping should be used to create a constant strain rate in the specimen
- Dispersion correction and time shifting of the data should be performed
- 1-wave classical analysis seems to yield correct result when the above parameters are present

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